

## Warm-up

(Complete the following problems in notebook or on homework page.)

1. 2, 4, 12, 48, 240,  <sup>$\times 6$</sup> ? 1440

2. -5, -10,  <sup>$\times 2$</sup> -20, -40, ? -80

3. Determine if the conjecture is true or false, if false provide a counterexample.

Given:  <sup>$\angle 3$</sup>  and  $\angle 4$  are supplementary

<sup>$\angle 3$</sup>  and  $\angle 5$  are supplementary

Conjecture:  $\angle 4 \cong \angle 5$

## 2-2 Logic

Statement-Sentence that is either true or false, but not both

Truth value-whether it is true or false

Negation-opposite meaning as well as opposite truth value (Symbol  $\sim$ )

Example:

p: September has 30 days. I

not p or  $\sim p$ :

Sept. does not have 30 days.

(The letters p, q, and r are typically used to represent statements.)

Compound statement-- combine  
2 or more statements  
using AND + OR

q: September is the 9<sup>th</sup> month of the year.

p and q:

Sept. has 30 days and  
is the 9<sup>th</sup> month of the  
year.

AND-conjunction Symbol  $\wedge$   $p \wedge q$  "p and q"

True,  
when BOTH statements are true

False,  
when either statement is false or both  
false

r: A square has 4 congruent sides.

True or False

$p \wedge q$	$\frac{T}{T \quad T}$	$p \wedge r$	$\frac{T}{T \quad T}$	$\sim p \wedge r$	$\frac{\text{False}}{F \quad T}$
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OR-disjunction Symbol  $\vee$   $p \vee q$  "p or q"

True,  
when either statement is true or both  
true

False,  
when BOTH statements are false

True or False

$p \vee q$	$\frac{T}{T \quad T}$	$\sim p \vee \sim r$	$\frac{F}{F \quad F}$	$\sim q \vee r$	$\frac{T}{F \quad T}$
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Complete the following example on your own.

F p:  $\overline{AB}$  is proper notation for "line AB"

T q: centimeters are metric units

F r: 9 is a prime number

Determine the truth value for #s 1-5.

1. $p \vee q$	$\frac{T}{F \quad T}$	2. $r \vee q$	$\frac{T}{F \quad T}$	3. $p \wedge q$	$\frac{F}{F \quad T}$
4. $\sim p \vee q$	$\frac{T}{T \quad T}$	5. $p \vee r$	$\frac{F}{F \quad F}$		

## Truth Tables

Negation	
p	$\sim p$
T	F
F	T

Conjunction		
p	q	$p \wedge q$
T	T	T
T	F	F
F	T	F
F	F	F

Disjunction		
p	q	$p \vee q$
T	T	T
T	F	T
F	T	T
F	F	F

Tautology-Compound sentence that is always true.

Ex: You are in school, or you are not in school.

$\sim p \vee q$

p	q	$\sim p$	$\sim p \vee q$
T	T	F	T
T	F	F	F
F	T	T	T
F	F	T	T

$$\sim p \wedge \sim q$$

$p$	$q$	$\sim p$	$\sim q$	$\sim p \wedge \sim q$
T	T	F	F	F
T	F	F	T	F
F	T	T	F	F
F	F	T	T	T

3 Terms

$$p \vee (\sim q \wedge r)$$

$p$	$q$	$r$	$\sim q$	$(\sim q \wedge r)$	
T	T	T	F	F	T
T	F	T	T	T	T
T	T	F	F	F	T
T	F	F	T	F	T
F	T	T	F	F	F
F	F	T	T	T	T
F	T	F	F	F	F
F	F	F	T	F	F

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$$(p \vee q) \wedge \sim r$$

$p$	$q$	$r$	$\sim r$	$(p \vee q)$	
T	T	T	F	T	F
T	F	T	F	T	F
T	T	F	T	T	T
T	F	F	T	T	T
F	T	T	F	T	F
F	F	T	F	F	F
F	T	F	T	T	T
F	F	F	T	F	F

HW

p72-73

18-29(T or F only),

30-32